



Sanjay Ghodawat University, Kolhapur

2017-18

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FY M Sc.

School of Science

Semester II

MTS ~~502~~ 510

Partial Differential Equations

Max Marks: 100

May/June 2018

End Semester Examination (ESE)

Time: 3 Hrs.

2 June 2018

Instructions for Students: 1) All questions are compulsory
10:30 AM to 1:30 PM.

- | Q1 | Choose correct alternative for the following questions | Marks | COs |
|----|---|-------|-----|
| a) | Solution of $p^2 + q^2 = x + y$ is..... | 2 | CO1 |
| | a. $z = (a+x)^{3/2} + \frac{3}{2}(y-a)^{3/2} + b$ | | |
| | b. $z = \frac{2}{3}(a+x)^{3/2} + \frac{2}{3}(y-a)^{3/2} + b$ | | |
| | c. $z = \frac{3}{2}(a+x)^{3/2} + \frac{3}{2}(y-a)^{3/2} + b$ | | |
| | d. None of these | | |
| b) | A. The solution of ordinary differential equation of order n have n arbitrary constants
B. The solution of partial differential equation of order n has n arbitrary functions
a. A is true, B is false b. A is false, B is true
c. Both A and B are true d. Both A and B are false | 2 | CO1 |
| c) | The relation $z = (x+a)(y+b)$ represents the partial differential equation | 2 | CO2 |
| | a. $z = \frac{p}{q}$ b. $z = pq$
c. $z = p - q$ d. none of these | | |
| d) | A solution of $u_{xx} = 0$ is of the form..... | 2 | CO3 |
| | a) $u = \int f(y)dx + \phi(y)$ b) $u = \int (f'(y)dy + f(y)dx)$
c) $u = \int f(y)dx$ d) $u = \int (f(x)dx + f(y)dy)$ | | |
| e) | The heat equation is..... | 2 | CO4 |
| | a) $\frac{\partial u}{\partial x} = c^2 \nabla^2 x^2$ b) $\frac{\partial u}{\partial y} = \frac{\nabla^2 t^2}{c^2}$
c) $\frac{\partial u}{\partial t} = c^2 \nabla^2 u$ d) $\frac{\partial u}{\partial t} = c^2 \nabla^2 y^2$ | | |
| f) | The differential equation $f_{xx} + 2f_{xy} + 4f_{yy} = 0$ is classified as | 2 | CO3 |

	a) Hyperbolic c) Elliptic	b) Parabolic d) None of these		
Q2	Attempt any two of the following			
a)	By a suitable change of independent variables, show that a second order p.d.e $Rr + Ss + Tt + g(x, y, x, u_x, u_y) = 0$ can be reduced to one of the canonical form on the basis of $S^2 - 4RT = 0$	10	CO3	
b)	By separable variable method, find the solution equation $\frac{\partial u}{\partial t} = k \frac{\partial^2 u}{\partial x^2}, 0 < x < l, t > 0$ satisfying the conditions $u(0, t) = 0, u(l, t) = 0, t > 0$ and $u(x, 0) = f(x), 0 < x < l$	10	CO4	
c)	Solve $\nabla^2 u = 0, 0 \leq x \leq a, 0 \leq y \leq b$, subject to the boundary condition $u_x(0, y) = u_x(a, y) = 0, u_y(x, 0) = 0, u_y(x, b) = f(x)$	10	CO5	
Q3	Attempt any two of the following			
a)	Find the complete integrals by charpits method $(p^2 + q^2)y - qz = 0$	8	CO2	
b)	Find the condition that a one parameter family of surfaces form a family of equipotential surfaces	8	CO4	
c)	Solve $\nabla^2 u = 0, r < a$ subject to the boundary condition $\frac{\partial u}{\partial n} = \frac{\partial u}{\partial n} = f(\theta)$ on $r = a$ where $\int_0^{2\pi} f(\theta) d\theta = 0$	8	CO5	
Q4	Attempt any two of the following			
a)	Find the direction cosines of the tangent of the curve $x = x(s), y = y(s), z = z(s)$ where s is arc length of the curve measured from the fixed point P_0 on the curve to any point P on the curve are $\left(\frac{dx}{ds}, \frac{dy}{ds}, \frac{dz}{ds}\right)$	6	CO1	
b)	Solve the equations by Jacobi's method $z^2 + zu_z - u_x^2 - u_y^2 = 0$	6	CO2	
c)	Write short note on classification of second order p.d.e and its canonical forms.	6	CO3	
Q5	Attempt any three of the following			
a)	Find the direction cosines of the normal to the surface S of the form $z = f(x, y)$	4	CO1	

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|----|--|---|-----|
| b) | Obtain the partial differential equation of first order by elimination arbitrary constants from the relation $(x-a)^2 + (y-b)^2 + z^2 = 1$ | 4 | CO1 |
| c) | Write short note on types of some standard types of first order differential equations | 4 | CO2 |
| d) | Prove that the solution of the Dirichlet problem, if it exists, is unique | 4 | CO5 |

Q6

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|-----------------------------------|---|---|-----|
| Attempt any four of the following | | | |
| a) | Show that following Pfaffian differential equations are integrable and hence find its corresponding integral.
$(y^2 + yz)dx + (xz + z^2)dy + (y^2 - xy)dz = 0$ | 7 | CO1 |
| b) | Describe the charpit's method of a solving a first order partial differential equations $f(x,y,z,p,q)=0$ | 7 | CO2 |
| c) | Reduce the equations to Canonical form $x^2 u_{xx} - y^2 u_{yy} = 0$ | 7 | CO3 |
| d) | Show that the following surfaces form a family of equipotential surfaces and find general form of the corresponding potential function
$(x^2 + y^2)^2 - 2a^2(x^2 + y^2) + a^4 = c$ | 7 | CO4 |
| e) | Stability Theorem :Show that the solution of the Dirichlet problem is stable | 7 | CO5 |
